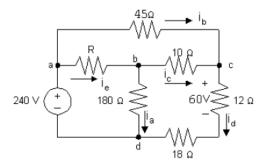
EE 215 Fundamentals of Electrical Engineering Problem #2 Solution

Spring 2010

P 2.24



$$\begin{split} i_{\rm d} &= 60/12 = 5\,\mathrm{A}; \quad \text{therefore, } v_{\rm cd} = 60 + 18(5) = 150\,\mathrm{V} \\ -240 + v_{\rm ac} + v_{\rm cd} = 0; \quad \text{therefore, } v_{\rm ac} = 240 - 150 = 90\,\mathrm{V} \\ i_{\rm b} &= v_{\rm ac}/45 = 90/45 = 2\,\mathrm{A}; \quad \text{therefore, } i_{\rm c} = i_{\rm d} - i_{\rm b} = 5 - 2 = 3\,\mathrm{A} \\ v_{\rm bd} &= 10i_{\rm c} + v_{\rm cd} = 10(3) + 150 = 180\,\mathrm{V}; \\ \text{therefore, } i_{\rm a} &= v_{\rm bd}/180 = 180/180 = 1\,\mathrm{A} \\ i_{\rm e} &= i_{\rm a} + i_{\rm c} = 1 + 3 = 4\,\mathrm{A} \\ -240 + v_{\rm ab} + v_{\rm bd} = 0 \quad \text{therefore, } v_{\rm ab} = 240 - 180 = 60\,\mathrm{V} \\ R &= v_{\rm ab}/i_{\rm e} = 60/4 = 15\,\Omega \\ \text{CHECK:} \quad i_g &= i_{\rm b} + i_{\rm e} = 2 + 4 = 6\,\mathrm{A} \\ p_{\rm dev} &= (240)(6) = 1440\,\mathrm{W} \\ \sum P_{\rm dis} &= 1^2(180) + 4^2(15) + 3^2(10) + 5^2(12) + 5^2(18) + 2^2(45) \\ &= 1440\,\mathrm{W} \,\, \text{(CHECKS)} \end{split}$$

P 2.27 [a] $i_o = 0$ because no current can exist in a single conductor connecting two parts of a circuit.

[b]

$$18 \lor \begin{array}{c} & & & & \\$$

$$18 = (12+6)i_g$$
 $i_g = 1$ A
 $v_{\Delta} = 6i_g = 6$ V $v_{\Delta}/2 = 3$ A
 $10i_1 = 5i_2$, so $i_1 + 2i_1 = -3$ A; therefore, $i_1 = -1$ A

[c]
$$i_2 = 2i_1 = -2$$
 A.

P 3.5 [a]
$$R_{ab} = 10 + (5||20) + 6 = 10 + 4 + 6 = 20 \Omega$$

[b] $R_{ab} = 30 \text{ k}||60 \text{ k}||[20 \text{ k} + (200 \text{ k}||50 \text{ k})] = 30 \text{ k}||60 \text{ k}||(20 \text{ k} + 40 \text{ k})$
 $= 30 \text{ k}||60 \text{ k}||60 \text{ k} = 15 \text{ k}\Omega$

P 3.13 [a]
$$R_{eq} = R || R = \frac{R^2}{2R} = \frac{R}{2}$$

[b] $R_{eq} = R || R || R || \cdots || R$ ($n R$'s)
$$= R || \frac{R}{n-1}$$

$$= \frac{R^2/(n-1)}{R+R/(n-1)} = \frac{R^2}{nR} = \frac{R}{n}$$

[c]
$$\frac{R}{2} = 5000$$
 so $R = 10~\mathrm{k}\Omega$
This is a resistor from Appendix H.

[d]
$$\frac{R}{n}=4000$$
 so $R=4000n$
If $n=3$ $r=4000(3)=12$ k Ω
This is a resistor from Appendix H. So put three 12k resistors in parallel to get $4k\Omega$.

P 3.20
$$\frac{(24)^2}{R_1 + R_2 + R_3} = 80$$
, Therefore, $R_1 + R_2 + R_3 = 7.2 \Omega$
$$\frac{(R_1 + R_2)24}{(R_1 + R_2 + R_3)} = 12$$

Therefore,
$$2(R_1 + R_2) = R_1 + R_2 + R_3$$

Thus,
$$R_1 + R_2 = R_3$$
; $2R_3 = 7.2$; $R_3 = 3.6 \Omega$

$$\frac{R_2(24)}{R_1 + R_2 + R_3} = 5$$

$$4.8R_2 = R_1 + R_2 + 3.6 = 7.2$$

Thus,
$$R_2 = 1.5 \Omega$$
; $R_1 = 7.2 - R_2 - R_3 = 2.1 \Omega$

P 3.28
$$5\Omega \| 20\Omega = 4\Omega;$$
 $4\Omega + 6\Omega = 10\Omega;$ $10\| (15 + 12 + 13) = 8\Omega;$

Therefore,
$$i_g = \frac{125}{2+8} = 12.5 \text{ A}$$

$$i_{6\Omega} = \frac{8}{6+4}(12.5) = 10 \text{ A}; \quad i_o = \frac{5||20|}{20}(10) = 2 \text{ A}$$

P 3.30 [a] The voltage across the
$$9\Omega$$
 resistor is $1(12+6)=18$ V.

The current in the 9Ω resistor is 18/9 = 2 A. The current in the 2Ω resistor is 1 + 2 = 3 A. Therefore, the voltage across the 24Ω resistor is (2)(3) + 18 = 24 V.

The current in the 24Ω resistor is 1 A. The current in the 3Ω resistor is 1+2+1=4 A. Therefore, the voltage across the 72Ω resistor is 24+3(4)=36 V.

The current in the 72Ω resistor is 36/72 = 0.5 A.

The $20\,\Omega\|5\,\Omega$ resistors are equivalent to a $4\,\Omega$ resistor. The current in this equivalent resistor is 0.5+1+3=4.5 A. Therefore the voltage across the $108\,\Omega$ resistor is 36+4.5(4)=54 V.

The current in the $108\,\Omega$ resistor is 54/108=0.5 A. The current in the $1.2\,\Omega$ resistor is 4.5+0.5=5 A. Therefore,

$$v_q = (1.2)(5) + 54 = 60 \text{ V}$$

[b] The current in the $20\,\Omega$ resistor is

$$i_{20} = \frac{(4.5)(4)}{20} = \frac{18}{20} = 0.9 \text{ A}$$

Thus, the power dissipated by the $20\,\Omega$ resistor is

$$p_{20} = (0.9)^2(20) = 16.2 \text{ W}$$

P 3.43 [a]
$$v_{\text{meter}} = 180 \text{ V}$$

[b]
$$R_{\text{meter}} = (100)(200) = 20 \text{ k}\Omega$$

$$20||70 = 15.555556 \text{ k}\Omega$$

$$v_{\text{meter}} = \frac{180}{35.555556} \times 15.555556 = 78.75 \text{ V}$$

[c]
$$20||20 = 10 \text{ k}\Omega$$

$$v_{\text{meter}} = \frac{180}{80}(10) = 22.5 \text{ V}$$

[d]
$$v_{\text{meter a}} = 180 \text{ V}$$

$$v_{\text{meter b}} + v_{\text{meter c}} = 101.26 \text{ V}$$

No, because of the loading effect.

P 3.45 [a]
$$R_1 = (100/2)10^3 = 50 \text{ k}\Omega$$

$$R_2 = (10/2)10^3 = 5 \text{ k}\Omega$$

$$R_3 = (1/2)10^3 = 500 \,\Omega$$

[b] Let
$$i_{\rm a}$$
 = actual current in the movement

 $i_{\rm d}$ = design current in the movement

Then % error
$$= \left(\frac{i_a}{i_d} - 1\right) 100$$

For the 100 V scale:

$$i_{\rm a} = \frac{100}{50,000 + 25} = \frac{100}{50,025}, \qquad i_{\rm d} = \frac{100}{50,000}$$

$$\frac{i_{\rm a}}{i_{\rm d}} = \frac{50,000}{50,025} = 0.9995 \qquad \% \text{ error } = (0.9995 - 1)100 = -0.05\%$$

For the 10 V scale:

$$\frac{i_{\rm a}}{i_{\rm d}} = \frac{5000}{5025} = 0.995$$
 % error = $(0.995 - 1.0)100 = -0.4975\%$

For the 1 V scale:

$$\frac{i_{\text{a}}}{i_{\text{d}}} = \frac{500}{525} = 0.9524$$
 % error = $(0.9524 - 1.0)100 = -4.76\%$